Local and tunable geometric phase of Dirac fermions in a topological junction

S.-J. Choi¹, S. Park¹, and H.-S. Sim¹

¹Department of Physics, Korea Advanced Institute of Science and Technology, Daejeon 305-701, Korea

Electrons in graphene and a surface of topological insulators behave as Dirac fermions (DFs). They have the interesting property of spin-momentum locking that their spin rotates following the change of the spatial momentum. Massless DFs acquire the Berry phase of π in the spatial motion along a closed trajectory on a plane, as their spin rotates along a great circle on Bloch sphere. This special value π causes topological phenomena [1, 2, 3] such as the half-integer quantum Hall effect and weak antilocalization.

When DFs become massive, they can have the other possible values of Berry phase of spin 1/2. The continuous values of Berry phase give rise to the modification of the known effects of Berry phase π . They may also result in new interesting effects, together with unusual transport of DFs, and will offer a way of experimentally detecting Berry phase of spin 1/2 in a controlled fashion.

We theoretically show that DFs acquire geometric phase as a scattering phase shift in a *local and nonadiabatic scattering* event of reflection or transmission at a junction with mass gap (See Fig. 1). The geometric phase of spin 1/2 is an electronic analogue of polarized light in optics [4, 5, 6]. The Pancharatnam-Berry phase has new roles in solids. It carries the information of the Chern number of the insulator side of a metal-insulator junction of DFs. This implies a new type of bulk-edge correspondence for a *metal-insulator* junction, which is different from the conventional version of the correspondence

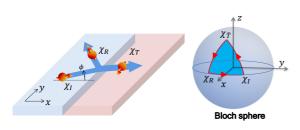


Figure 1: (left) Scattering of DFs at a junction with mass gap. A plane wave with a spin state χ_I incident from the left side is reflected to a wave with a spin state χ_R or transmitted to a wave with a spin state with χ_T . (right) The reflection coefficient of the scattering is shifted by geometric phase which amount is given by $-\Omega_{I\bar{T}R}/2$. $\Omega_{I\bar{T}R}$ is the solid angle of the geodesic polygon on the Bloch sphere which sequentially connects the vertices representing spin states χ_I , $\chi_{\bar{T}}$, χ_R , where $\chi_{\bar{T}}$ denotes the spin state orthogonal to χ_T .

with gapless edge states between two insulators with different Chern numbers. The Pancharatnam-Berry phase also modifies the quantization rule of DFs. This suggests geometric-phase devices with non-trivial charge and spin transport such as a topological wave guide and a topological field effect transistor.

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